

Polynômes

$$p = \sum_{i=0}^n a_i \cdot X^i = a_0 + a_1 X + a_2 X^2 + \dots + a_n X^n$$

Annotations:
 - n : jusqu'à a
 - a_0 : terme constant ($X^0 = 1$)
 - $\sum_{i=0}^n$: somme de
 - $a_i \in \mathbb{R}$

Exemple: $p = 1 + X + X^2$

$$= a_0 + a_1 X + a_2 X^2$$

$$= 1 + 1X + 1X^2$$

$$a_0 = 1$$

$$a_1 = 1$$

$$a_2 = 1$$

$\alpha \beta \gamma \dots \sigma$

\sum
 \uparrow
 signe maj.

$$q = -1 + 2X - 3X^2 + 4X^3 + 5X^4 - X^5$$

$$q = \underbrace{(-1)}_{a_0} X^0 + \underbrace{(2)}_{a_1} X^1 + \underbrace{(-3)}_{a_2} X^2 + \underbrace{(4)}_{a_3} X^3 + \underbrace{(5)}_{a_4} X^4 + \underbrace{(-1)}_{a_5} X^5$$

$$q = [-1, 2, -3, 4, 5, -1]$$

\uparrow
 $q[0]$

\uparrow
 $q[1]$

\uparrow
 $q[5]$

$$q = \sum_{i=0}^n q[i] \cdot X^i$$

Maths

$$p(x) = x^4 - 3x^3 + 2x^2 + x - 1$$

$$q(x) = x^4 + 3x^3 - 2x^2 + 3x + 4$$

$$p(x) + q(x) = 2x^4 + 4x + 3$$

$$r(x) = x^2 - 2x + 3$$

$$\begin{aligned} p(x) + r(x) &= r(x) + p(x) \\ &= x^4 - 3x^3 + 3x^2 - x + 2 \end{aligned}$$

Machine

$$p = \begin{matrix} p[0] & p[1] & \dots \\ [-1, & 1, & 2, & -3, & 1] \\ x^0 & x^1 & x^2 & x^3 & x^4 \end{matrix}$$

$$q = [4, 3, -2, 3, 1]$$

$$\text{somme}(p, q) = [3, 4, 0, 0, 2]$$

$$r = [3, -2, 1]$$

$$r = [3, -2, 1, 0, 0]$$

$$p = [-1, 1, 2, -3, 1]$$

P·q

	-1	1	2	-3	1
4	-4	4	8	-12	4
3	-3	3	6	-9	3
-2	2	-2	-4	6	-2
3	-3	3	6	-9	3
1	-1	1	2	-3	1