

Dérivée et géométrie

$$-b/2a = \frac{3}{4}$$

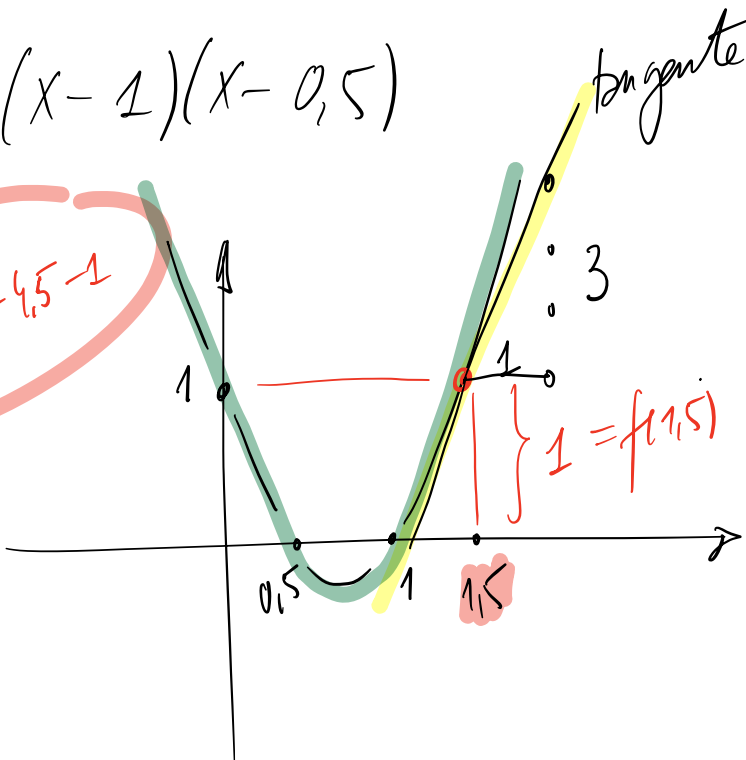
$$f(x) = 2x^2 - 3x + 1$$

$$f'(x) = 2 \cdot 2x - 3 = 4x - 3$$

$$x = \frac{3 \pm \sqrt{9 - 8}}{4} = \begin{cases} 1 \\ 1/2 \end{cases}$$

$$x = \frac{3}{4}$$

$$2(x-1)(x-0,5)$$

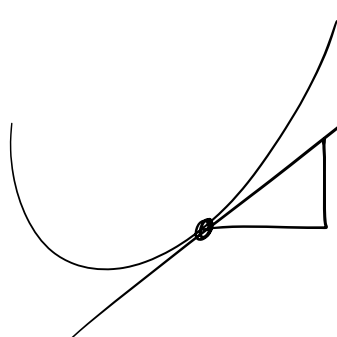


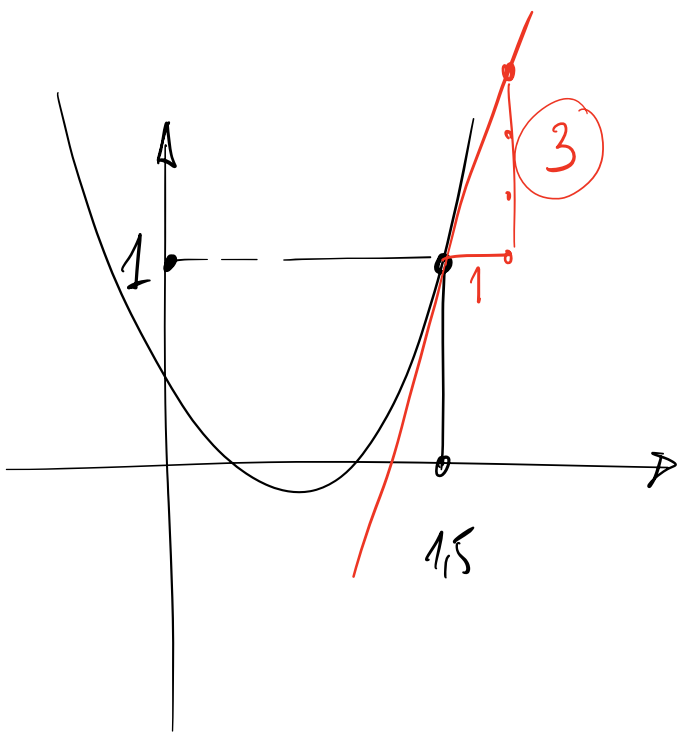
$$f(1,5) = 4 \cdot 1,5 - 4,5 - 1$$

$$f'(x) = 4x - 3$$

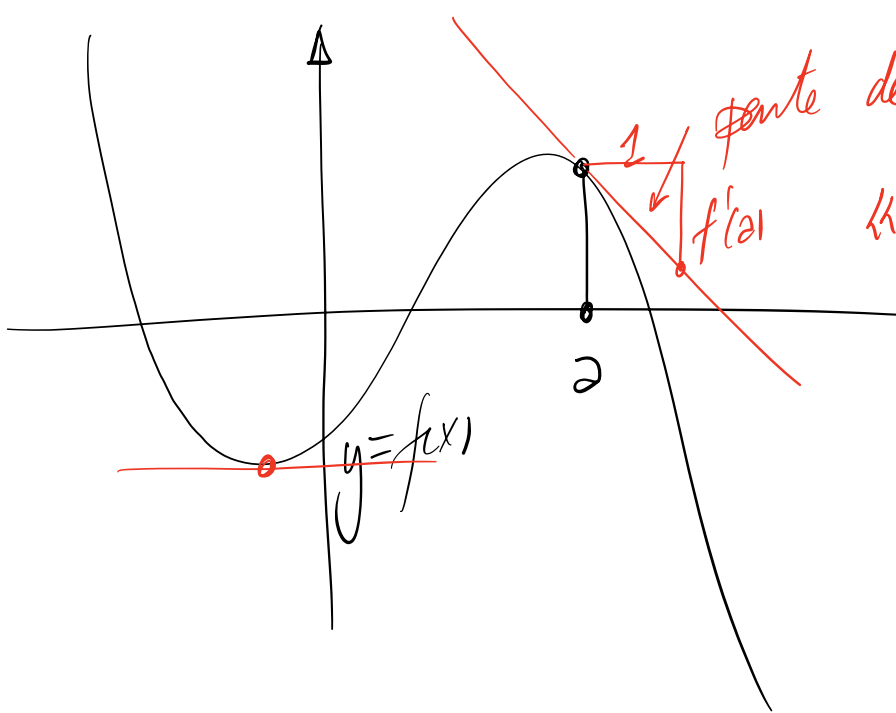
$$x = 1,5$$

$$f'(1,5) = 4 \cdot 1,5 - 3 = 3$$

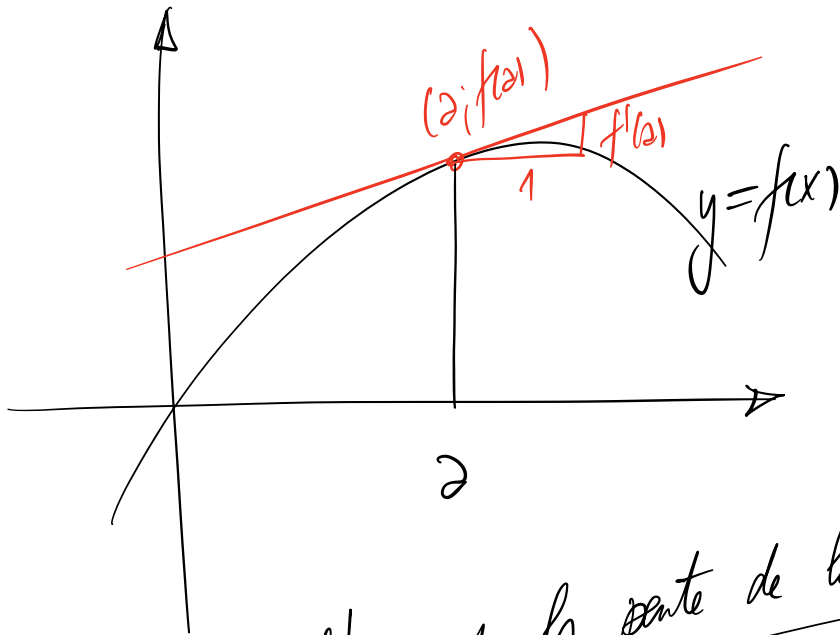

 pente de la tangente = dérivée



pente de la tangente: 3
 ↑
 $f'(1.5)$



pente de la tangente
 « en dessous de 2 »
 $f'(2)$



$f'(a)$ est la pende de la tangente au point $(a, f(a))$

$$\left(\frac{1}{x} + \frac{1}{2x^2} + \frac{1}{3x^3}\right)' = \left(\frac{1}{x}\right)' + \left(\frac{1}{2x^2}\right)' + \left(\frac{1}{3x^3}\right)'$$

$$\frac{1^0 \cdot x - 1 \cdot x^1}{x^2} + \frac{1^0 \cdot 2x^2 - 1 \cdot (2x^2)'}{(2x^2)^2} + \frac{1^0 \cdot 3x^3 - 1 \cdot (3x^3)'}{(3x^3)^2} =$$

$$\frac{-1}{x^2} + \frac{-2 \cdot 2x}{4x^4} + \frac{-3 \cdot 3x^2}{9x^6} =$$

$$\frac{-1}{x^2} - \frac{1}{x^3} - \frac{1}{x^4}$$

$$\left(\frac{1}{\sin x \cos x} \right)' = \frac{\overbrace{1' \cdot \sin x - \cos x}^0 - 1 \cdot (\sin x \cos x)'}{(\sin x \cos x)^2}$$

$$= \frac{-((\sin x)' \cdot \cos x + \sin x \cdot (\cos x)')}{(\sin x \cos x)^2}$$

$$(f \cdot g)' = f'g + fg'$$