

$$\int_{-1}^1 x \sqrt{1-x^2} dx = \int_{-1}^1 \underbrace{(1-x^2)^{\frac{1}{2}}}_{()'} \cdot x \cdot dx$$

$$(-2x) = (1-x^2)'$$

$$= -\frac{1}{2} \int_{-1}^1 (1-x^2)^{\frac{1}{2}} \cdot (-2x) \cdot dx = -\frac{1}{2} \int_{-1}^1 (1-x^2)^{\frac{1}{2}} \cdot \underbrace{(1-x^2)'}_{()'} dx$$

$$\int T^{\frac{1}{2}} dT = \frac{1}{1+\frac{1}{2}} T^{1+\frac{1}{2}} = \frac{2}{3} T^{\frac{3}{2}}$$

$$= -\frac{1}{2} \cdot \left(\frac{2}{3} (1-x^2)^{\frac{3}{2}} \right) \Big|_{-1}^1$$

$$(u(v(x)))' = u'(v(x)) \cdot v'(x)$$

$$\left(\frac{2}{3} (1-x^2)^{\frac{3}{2}} \right)' = \cancel{\frac{2}{3}} \cdot \cancel{\frac{3}{2}} \cdot (1-x^2)^{\frac{3}{2}-1} \cdot (1-x^2)'$$

$$\int dx \quad (x^n)' = n x^{n-1} = (1-x^2)^{\frac{1}{2}} \cdot (-2x)$$

$$\left(\frac{2}{3} (1-x^2)^{\frac{3}{2}} \right)' = (1-x^2)^{\frac{1}{2}} \cdot (-2x)$$

$(1-x^2)' = -2x$

$$\frac{2}{3} (1-x^2)^{\frac{3}{2}} = \int (1-x^2)^{\frac{1}{2}} (-2x) dx$$

$$\left(\ln(x^2+2x-1) \right)' = \frac{1}{x^2+2x-1} \cdot (x^2+2x-1)'$$

$$u(v(x))$$

$$= \frac{2x+2}{x^2+2x-1}$$

$$u(x) = \ln(x)$$

$$v(x) = x^2+2x-1$$

$$\int 5x \, dx = \frac{1}{5} \int (5x)^1 \cdot 5 \, dx = \frac{1}{5} \int (5x)^1 \cdot (5x)' \, dx$$

$$= \frac{1}{5} \cdot \frac{1}{1+1} \cdot (5x)^{1+1} = \frac{1}{5} \cdot \frac{1}{2} \cdot (5x)^2$$

$$= \frac{1}{5} \cdot 25x^2 = \frac{5}{2}x^2$$

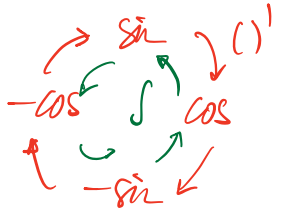
$$\int 5x \, dx = 5 \int x \, dx = 5 \cdot \frac{1}{1+1} \cdot x^{1+1}$$

$$= \frac{5}{2}x^2$$

$$\int_a^b f(x) dx = \int_a^c f(x) dx + \int_c^b f(x) dx$$

$$\int_a^b f(x) dx = - \int_b^a f(x) dx$$

$$\int (-\cos(3x)) dx = -\frac{1}{3} \int \cos(3x) \cdot \underbrace{3}_{(3x)'} dx$$



$$= -\frac{1}{3} \cdot \sin(3x) + C$$

$$f''(x) = 3x$$

$$f'(x) = \frac{3}{2}x^2 + C \quad \frac{3}{2}x^2 + C = 0 / C = -\frac{3}{2}$$

$$f'(1) = 0$$

$$f(x) = \frac{3}{2} \cdot \frac{1}{3} \cdot x^3 + Cx + d$$

$$f(2) = 1$$

$$f(x) = \frac{1}{2}x^3 - \frac{3}{2}x + d$$

$$\frac{1}{2}2^3 - \frac{3}{2} \cdot 2 + d = 1$$