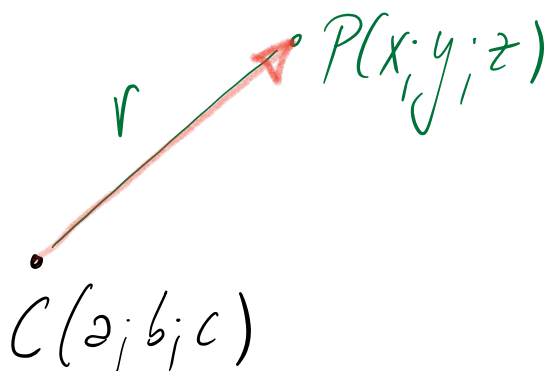


$r \in ]0; +\infty[$



sphere  
 $\Sigma(a, b, c, r)$

$$u = \begin{pmatrix} x - a \\ y - b \\ z - c \end{pmatrix}$$

$$P \text{ est sur } \Sigma \Leftrightarrow \|u\| = r \Leftrightarrow \|u\|^2 = r^2$$

$$(x-a)^2 + (y-b)^2 + (z-c)^2 = r^2$$

Eq. du cercle dans  $\mathbb{R}^3$ :  $\Sigma \cap \pi$

$$\Sigma : (x-a)^2 + (y-b)^2 + (z-c)^2 = r^2$$

$a, b, c, e, f, g, h \in \mathbb{R}$

$$\pi : ex + fy + gz + h = 0$$

$$x^2 + y^2 + z^2 - 12x - 2y + 6z + 56 = 0$$

$$A^2 - 2AB + B^2 - B^2 = (A-B)^2 - B^2$$

$$x^2 - 12x + y^2 - 2y + z^2 + 6z = -56$$

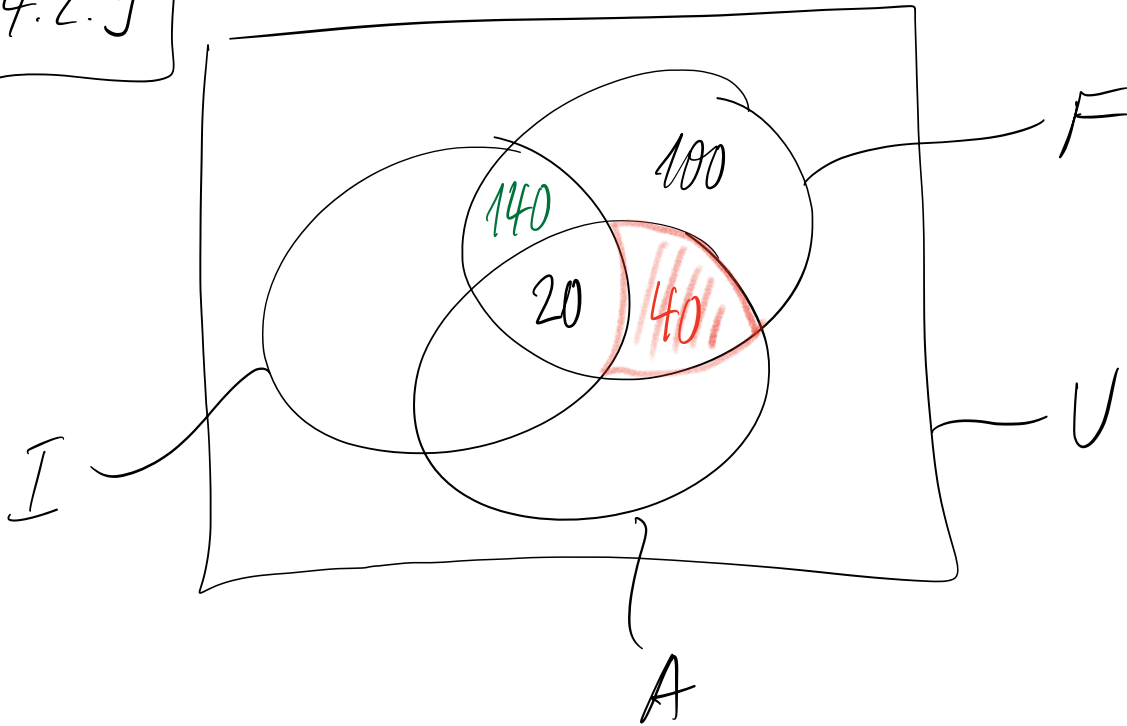
$$\underbrace{x^2 - 2 \cdot x \cdot 6 + 6^2 - 6^2}$$

$$(x-6)^2 - 6^2 + (y-1)^2 - 1 + (z+3)^2 - 9 = -56$$

$$(x-6)^2 + (y-1)^2 + (z+3)^2 = 36 + 1 + 9 - 56 = \underbrace{-10}_{r^2}$$

Ce n'est pas une sphère car  $r^2$  est positif.

4.2.9



4.3.2

A : coeur  $P(A) = \frac{9}{36} = \frac{1}{4}$

B : valet de coeur  $P(B) = \frac{1}{36}$

$$P(A \cap B) = \frac{1}{36} = P(B \cap A)$$

$$P(B|A) = \frac{P(B \cap A)}{P(A)} = \frac{\frac{1}{36}}{\frac{9}{36}} = \frac{1}{9}$$