

Matrice

$$M = \begin{pmatrix} 1 & -2 \\ 3 & 2 \end{pmatrix} \quad \text{dimension 2}$$

$$\det M = \begin{vmatrix} 1 & -2 \\ 3 & 2 \end{vmatrix} = 1 \cdot 2 - 3 \cdot (-2) \\ \uparrow \\ \text{determinant} = 2 + 6 = 8$$

$$\begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc \in \mathbb{R}$$

dimension 3

$$M = \begin{pmatrix} 1 & -2 & 1 \\ 3 & 2 & 1 \\ 1 & -1 & 2 \end{pmatrix}$$

$1+1=2$ pair
 $2+1=3$ (impair)
 $3+1=4$ pair

pas de changement de signe
 changement de signe
 pas de changement

$$\det M = 2 \cdot \begin{vmatrix} 1 & -2 & 1 \\ 3 & 2 & 1 \\ 1 & -1 & 2 \end{vmatrix} = 2 \cdot 1 \cdot \begin{vmatrix} 2 & 1 \\ -1 & 2 \end{vmatrix} = 2 \cdot (-3) \cdot \begin{vmatrix} -2 & 1 \\ -1 & 2 \end{vmatrix} = 2 \cdot (-3) \cdot (5 + 9 - 4) = -6 \cdot 10 = -60$$