

2.8.11

$$f) \sqrt{(4x^2 - 2x)^3} = \left[(4x^2 - 2x)^3 \right]^{\frac{1}{2}}$$

$$= (4x^2 - 2x)^{\frac{3}{2}}$$

$$f'(x) = \left[(4x^2 - 2x)^{\frac{3}{2}} \right]' = \frac{3}{2} (4x^2 - 2x)^{\frac{1}{2}} \cdot (4x^2 - 2x)'$$

$$= \frac{3}{2} (8x - 2) \sqrt{4x^2 - 2x}$$

$$= (12x - 3) \sqrt{4x^2 - 2x} = 3(4x - 1) \sqrt{4x^2 - 2x}$$

2.8.1 d)

$$f(x) = \frac{1}{3x+1}$$

$$\frac{f(x+h) - f(x)}{h} = \frac{\left[\frac{1}{3(x+h)+1} - \frac{1}{3x+1} \right]}{h}$$

$$= \frac{1}{h} \cdot \left[\frac{1 \cdot (3x+1) - (3(x+h)+1) \cdot 1}{(3(x+h)+1)(3x+1)} \right]$$

$$= \frac{1}{h} \cdot \frac{\cancel{3x+1} - \overbrace{3(x+h)} - \cancel{1}}{(3(x+h)+1)(3x+1)} = \frac{1}{h} \cdot \frac{\cancel{3x} - \cancel{3x} - 3h}{(3(x+h)+1)(3x+1)}$$

$$= \frac{1}{\cancel{h}} \cdot \frac{(-3) \cdot h}{(3(x+h)+1)(3x+1)} = - \frac{3}{(3(x+h)+1)(3x+1)}$$

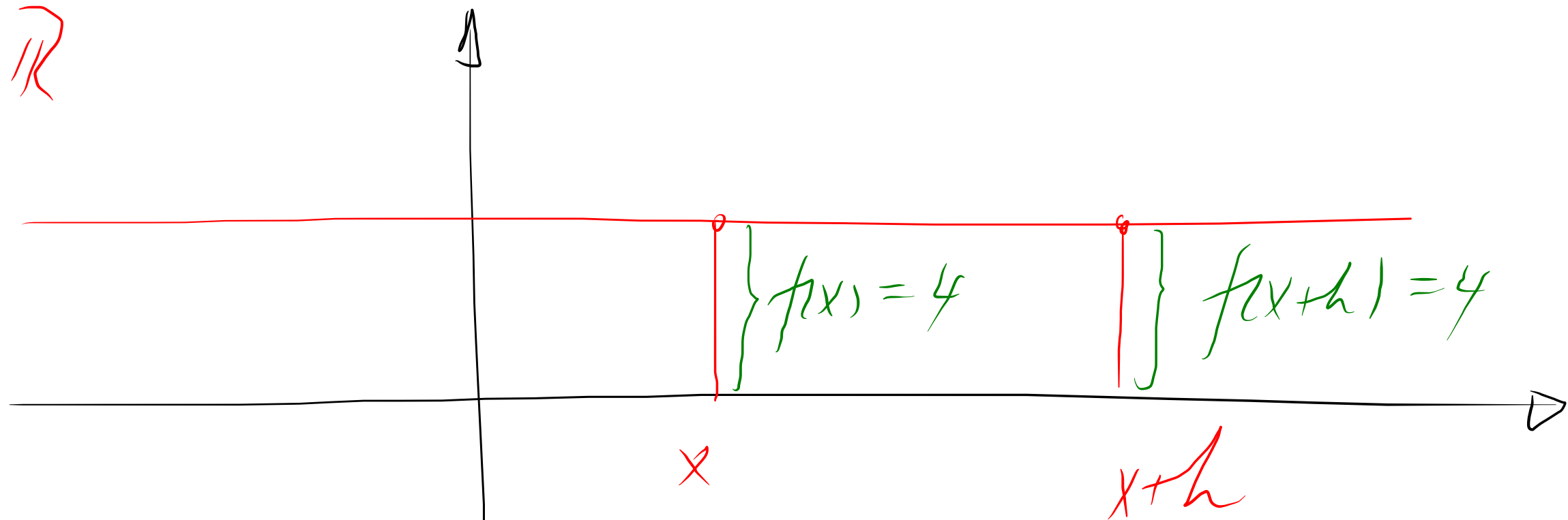
$\downarrow h \rightarrow 0$

$$= - \frac{3}{(3x+1)^2}$$

$$\frac{f(x+h) - f(x)}{h} \xrightarrow{h \rightarrow 0} f'(x)$$

$$f(x) = 4 \quad \forall x \in \mathbb{R}$$

$$f(x+h) = 4$$



$$\frac{f(x+h) - f(x)}{h} = \frac{4 - 4}{h} = \frac{0}{h} = 0 \xrightarrow{h \rightarrow 0} 0$$

$$\Rightarrow (4)' = 0$$

$$\left(\frac{\sin x + 1}{1 - \sin x} \right)'$$

$$= \frac{\overset{f'}{1} \cos x (1 - \overset{g}{\sin x}) - (\sin x + 1) (-\overset{g'}{\cos x})}{(1 - \sin x)^2}$$

2.8.12

f)

$$= \frac{\cos x - \cancel{\sin x \cos x} - \cancel{\sin x \cos x} + \cos x}{(1 - \sin x)^2}$$

$$= \frac{2 \cos x}{(1 - \sin x)^2}$$

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