

$$\begin{aligned}
c) \quad F'(x) &= \left[2x \cdot (x+1)^{-\frac{1}{2}} \right]' \\
&= (2x)' \cdot (x+1)^{-\frac{1}{2}} + 2x \cdot \left[(x+1)^{-\frac{1}{2}} \right]' \\
&= 2 \cdot (x+1)^{-\frac{1}{2}} - 2x \cdot \frac{1}{2} (x+1)^{-\frac{1}{2}-1} \\
&= 2(x+1)^{-\frac{1}{2}} - x(x+1)^{-\frac{3}{2}} \\
&= \frac{2}{\sqrt{x+1}} - \frac{x}{\sqrt{(x+1)^3}} \\
&= \frac{2\sqrt{(x+1)^2}}{\sqrt{x+1} \sqrt{(x+1)^2}} - \frac{x}{\sqrt{(x+1)^3}} \\
&= \frac{2x+2-x}{\sqrt{(x+1)^3}} = \frac{x+2}{\sqrt{(x+1)^3}}
\end{aligned}$$